

POWER SIMULATION FOR COX REGRESSION

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MODEL $\log(\text{hazard}) = \log(\text{baseline hazard}) + bx$

Survival times:

Two distributions, exponential and Weibull, were used to generate survival times

The following parametrizations were used:

Exponential survival times $\log(\text{baseline hazard}) = a$
Weibull survival times $\log(\text{integrated baseline hazard}) = a + c \log(\text{time})$

Censoring:

Uniform censoring on the interval from 1 - A to 1.

This censoring scheme mimics a trial in which patients enter uniformly from time 0 to time A and are followed until time 1.

The censored survival time was obtained as the minimum of the survival time and the censoring time.

Exponential survival times
Percent censored values for $x=0$

a	A=0.2	A=0.5	A=0.8
-1	71.8%	76.0%	80.5%
0	40.7%	47.7%	56.4%
1	8.8%	14.0%	23.7%

Weibull survival times, A = 0.5
Percent censored values for $x=0$

Shape	a	% cens.
0.2	-1.25	76.4%
0.2	-0.75	64.1%
0.2	-0.25	48.1%
0.5	-1.15	76.1%
0.5	-0.65	63.8%
0.5	-0.15	47.7%
2	-0.75	76.3%
2	-0.25	64.4%
2	0.25	49.1%
5	-0.1	76.4%
5	0.5	63.6%
5	1.1	48.4%

Covariate x

Covariate values were obtained as a sample from a standardized distribution.

Distribution considered: Normal, Uniform, Gamma(3) and Double Exponential

Simulated power and estimated power derived from equivalent two-sample test using either population values or sample values for mean and standard deviation of covariate

Sample size	Normal		Uniform		Gamma(3)	
	mean	s.d.	mean	s.d.	mean	s.d.
n=100	-0.0706	1.0821	-0.0845	1.0653	-0.0356	1.0765
n=200	-0.0482	1.0606	-0.0245	1.0433	-0.0264	0.9940
n=500	-0.0041	0.9747	0.0028	0.9902	-0.0146	0.9473
population	0.0000	1.0000	0.0000	1.0000	0.0000	1.0000

**POWER: NORMAL COVARIATE
EXPONENTIAL SURVIVAL TIMES**

sample size 100, a = -1

b	simulation	A = 0.2		A = 0.5			A = 0.8		
		formula population	formula sample	simulation	formula population	formula sample	simulation	formula population	formula sample
0.00	0.0523	0.0500	0.0500	0.0488	0.0500	0.0500	0.0502	0.0500	0.0500
0.05	0.0609	0.0581	0.0595	0.0595	0.0569	0.0581	0.0549	0.0556	0.0565
0.10	0.0888	0.0828	0.0883	0.0828	0.0779	0.0826	0.0755	0.0726	0.0764
0.15	0.1402	0.1252	0.1376	0.1256	0.1138	0.1243		0.1016	0.1101
0.20	0.2078	0.1857	0.2076		0.1652	0.1837	0.1592	0.1431	0.1581
0.25		0.2638	0.2967	0.2596	0.2319	0.2601		0.1972	0.2203
0.30	0.3996	0.3567	0.4005		0.3123	0.3507	0.2954	0.2633	0.2952
0.35		0.4593	0.5117	0.4551	0.4033	0.4507		0.3397	0.3803
0.40	0.6512	0.5648	0.6218		0.5000	0.5537	0.4819	0.4236	0.4716
0.45		0.6658	0.7224	0.6887	0.5967	0.6529		0.5112	0.5641
0.50	0.8375	0.7561	0.8076		0.6878	0.7424	0.6940	0.5983	0.6530
0.55	0.9023	0.8313	0.8744	0.8503	0.7687	0.8179		0.6807	0.7339
0.60	0.9448	0.8896	0.9229	0.9105	0.8364	0.8776	0.8418	0.7551	0.8038
0.65	0.9712	0.9319	0.9556	0.9474	0.8896	0.9219	0.9010	0.8190	0.8610
0.70	0.9880	0.9604	0.9760	0.9723	0.9292	0.9528	0.9385	0.8713	0.9056
0.75		0.9783	0.9878	0.9868	0.9568	0.9729	0.9659	0.9120	0.9385
0.80		0.9889	0.9942		0.9750	0.9853	0.9817	0.9423	0.9616

sample size 200, a = -1

b	simulation	A = 0.2		A = 0.5			A = 0.8		
		formula population	formula sample	simulation	formula population	formula sample	simulation	formula population	formula sample
0.00	0.0522	0.0500	0.0500	0.0497	0.0500	0.0500	0.0486	0.0500	0.0500
0.05	0.0662	0.0663	0.0683	0.0640	0.0639	0.0656	0.0595	0.0612	0.0626
0.10	0.1182	0.1166	0.1248	0.1071	0.1065	0.1135	0.0938	0.0958	0.1014
0.15		0.2031	0.2216		0.1800	0.1957		0.1551	0.1678
0.20	0.3523	0.3235	0.3543	0.3061	0.2833	0.3101	0.2588	0.2394	0.2615
0.25	0.4903	0.4668	0.5081		0.4100	0.4474		0.3455	0.3776
0.30	0.6473	0.6148	0.6605	0.5738	0.5473	0.5913	0.4914	0.4659	0.5062
0.35	0.7819	0.7476	0.7901	0.7141	0.6791	0.7236		0.5897	0.6339
0.40	0.8718	0.8514	0.8847	0.8223	0.7915	0.8303	0.7315	0.7051	0.7480
0.45	0.9357	0.9219	0.9441	0.8930	0.8766	0.9059		0.8027	0.8398
0.50	0.9751	0.9635	0.9762	0.9467	0.9338	0.9532	0.9033	0.8778	0.9063
0.55	0.9906	0.9849	0.9911	0.9786	0.9679	0.9791	0.9483	0.9301	0.9497
0.60		0.9945	0.9971	0.9916	0.9860	0.9917	0.9739	0.9632	0.9753
0.65		0.9982	0.9992		0.9945	0.9970	0.9902	0.9822	0.9889
0.70		0.9995	0.9998		0.9981	0.9991	0.9959	0.9921	0.9955

sample size 500, a = -1

b	simulation	A = 0.2		A = 0.5			A = 0.8		
		formula population	formula sample	simulation	formula population	formula sample	simulation	formula population	formula sample
0.00	0.0515	0.0500	0.0500	0.0544	0.0500	0.0500	0.0522	0.0500	0.0500
0.05	0.0844	0.0912	0.0891	0.0780	0.0850	0.0832	0.0727	0.0784	0.0769
0.10	0.2077	0.2205	0.2118	0.1835	0.1948	0.1873	0.1560	0.1671	0.1610
0.15	0.4052	0.4287	0.4110	0.3537	0.3759	0.3601	0.2927	0.3165	0.3032
0.20	0.6393	0.6604	0.6379	0.5637	0.5914	0.5695	0.4841	0.5063	0.4861
0.25	0.8221	0.8430	0.8240	0.7601	0.7820	0.7607	0.6743	0.6948	0.6723
0.30	0.9327	0.9452	0.9343	0.8909	0.9077	0.8929	0.8218	0.8422	0.8231
0.35	0.9815	0.9859	0.9815	0.9642	0.9696	0.9621	0.9248	0.9329	0.9204
0.40	0.9966	0.9973	0.9961	0.9900	0.9923	0.9895	0.9721	0.9768	0.9705

**POWER: NORMAL COVARIATE
EXPONENTIAL SURVIVAL TIMES**

sample size 100, a = 0

b	simulation	A = 0.2		A = 0.5			A = 0.8		
		formula population	formula sample	simulation	formula population	formula sample	simulation	formula population	formula sample
0.00	0.0507	0.0500	0.0500	0.0493	0.0500	0.0500	0.0481	0.0500	0.0500
0.05	0.0712	0.0671	0.0701	0.0700	0.0651	0.0677	0.0678	0.0626	0.0647
0.10	0.1316	0.1202	0.1321	0.1230	0.1117	0.1222	0.1108	0.1013	0.1100
0.15	0.2383	0.2113	0.2382	0.2182	0.1918	0.2155	0.1883	0.1678	0.1875
0.20	0.3766	0.3374	0.3818	0.3452	0.3039	0.3438		0.2620	0.2959
0.25	0.5489	0.4860	0.5444		0.4395	0.4938	0.4227	0.3790	0.4271
0.30	0.7053	0.6367	0.6995	0.6546	0.5828	0.6445		0.5088	0.5670
0.35	0.8254	0.7687	0.8248		0.7158	0.7751	0.7039	0.6377	0.6985
0.40	0.9068	0.8686	0.9104	0.8831	0.8243	0.8728		0.7526	0.8081
0.45	0.9614	0.9338	0.9601	0.9396	0.9021	0.9361	0.8968	0.8444	0.8889
0.50	0.9827	0.9706	0.9846	0.9738	0.9510	0.9717		0.9104	0.9418
0.55		0.9885	0.9949	0.9912	0.9781	0.9889	0.9746	0.9529	0.9724
0.60		0.9961	0.9985	0.9959	0.9913	0.9962	0.9894	0.9775	0.9882
0.65		0.9988	0.9996		0.9969	0.9988	0.9965	0.9902	0.9955
0.70		0.9997	0.9999		0.9990	0.9997	0.9983	0.9961	0.9984

sample size 200, a = 0

b	simulation	A = 0.2		A = 0.5			A = 0.8		
		formula population	formula sample	simulation	formula population	formula sample	simulation	formula population	formula sample
0.00	0.0527	0.0500	0.0500	0.0503	0.0500	0.0500	0.0506	0.0500	0.0500
0.05	0.0919	0.0846	0.0889	0.0851	0.0804	0.0842	0.0816	0.0753	0.0785
0.10	0.2059	0.1930	0.2108	0.1893	0.1757	0.1913	0.1667	0.1544	0.1674
0.15	0.3949	0.3721	0.4085	0.3558	0.3352	0.3681	0.3045	0.2886	0.3168
0.20	0.6201	0.5862	0.6341	0.5618	0.5339	0.5800	0.4809	0.4636	0.5061
0.25	0.8110	0.7770	0.8203	0.7604	0.7245	0.7704	0.6811	0.6464	0.6938
0.30	0.9260	0.9043	0.9318	0.8868	0.8659	0.8993	0.8243	0.8003	0.8408
0.35	0.9763	0.9679	0.9803	0.9598	0.9472	0.9652	0.9216	0.9049	0.9316
0.40	0.9933	0.9917	0.9958	0.9868	0.9834	0.9906	0.9686	0.9622	0.9760

sample size 500, a = 0

b	simulation	A = 0.2		A = 0.5			A = 0.8		
		formula population	formula sample	simulation	formula population	formula sample	simulation	formula population	formula sample
0.00	0.0497	0.0500	0.0500	0.0516	0.0500	0.0500	0.0467	0.0500	0.0500
0.05	0.1353	0.1382	0.1337	0.1218	0.1275	0.1236	0.1099	0.1145	0.1112
0.10	0.3867	0.4059	0.3890	0.3465	0.3658	0.3505	0.3008	0.3149	0.3018
0.15	0.6983	0.7331	0.7111	0.6458	0.6790	0.6566	0.5623	0.6010	0.5790
0.20	0.9159	0.9310	0.9185	0.8794	0.8985	0.8831	0.8158	0.8400	0.8209
0.25	0.9853	0.9905	0.9873	0.9728	0.9813	0.9760	0.9453	0.9585	0.9493
0.30	0.9985	0.9993	0.9989	0.9961	0.9981	0.9972	0.9901	0.9933	0.9908
0.35	1.0000	1.0000	1.0000	1.0000	0.9999	0.9998	0.9990	0.9993	0.9990
0.40	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	0.9998	1.0000	0.9999

**POWER: UNIFORM COVARIATE
EXPONENTIAL SURVIVAL TIMES**

sample size 100, a = -1

b	A = 0.2			A = 0.5			A = 0.8		
	simulation	formula population	formula sample	simulation	formula population	formula sample	simulation	formula population	formula sample
0.00	0.0523	0.0500	0.0500	0.0480	0.0500	0.0500	0.0481	0.0500	0.0500
0.05	0.0609	0.0581	0.0592	0.0537	0.0569	0.0578	0.0496	0.0556	0.0563
0.10	0.0888	0.0828	0.0871	0.0793	0.0779	0.0815	0.0701	0.0726	0.0755
0.15	0.1402	0.1252	0.1347	0.1169	0.1138	0.1218		0.1016	0.1081
0.20	0.2078	0.1857	0.2023		0.1652	0.1792	0.1463	0.1431	0.1544
0.25		0.2638	0.2885	0.2439	0.2319	0.2530		0.1972	0.2144
0.30	0.3996	0.3567	0.3892		0.3123	0.3407	0.2747	0.2633	0.2869
0.35		0.4593	0.4978	0.4335	0.4033	0.4379		0.3397	0.3693
0.40	0.6512	0.5648	0.6063		0.5000	0.5389	0.4555	0.4236	0.4581
0.45		0.6658	0.7067	0.6549	0.5967	0.6370		0.5112	0.5488
0.50	0.8375	0.7561	0.7931		0.6878	0.7266	0.6570	0.5983	0.6367
0.55	0.9023	0.8313	0.8620	0.8216	0.7687	0.8033		0.6807	0.7177
0.60	0.9448	0.8896	0.9132	0.8864	0.8364	0.8651	0.8073	0.7551	0.7885
0.65	0.9712	0.9319	0.9485	0.9290	0.8896	0.9119	0.8765	0.8190	0.8475
0.70	0.9880	0.9604	0.9713	0.9614	0.9292	0.9453	0.9162	0.8713	0.8943
0.75		0.9783	0.9849	0.9799	0.9568	0.9677	0.9511	0.9120	0.9295
0.80		0.9889	0.9926		0.9750	0.9819	0.9713	0.9423	0.9549

sample size 200, a = -1

b	A = 0.2			A = 0.5			A = 0.8		
	simulation	formula population	formula sample	simulation	formula population	formula sample	simulation	formula population	formula sample
0.00	0.0490	0.0500	0.0500	0.0478	0.0500	0.0500	0.0486	0.0500	0.0500
0.05	0.0652	0.0663	0.0677	0.0607	0.0639	0.0651	0.0587	0.0612	0.0622
0.10	0.1216	0.1166	0.1225	0.1064	0.1065	0.1115	0.0938	0.0958	0.0998
0.15		0.2031	0.2165		0.1800	0.1913		0.1551	0.1643
0.20	0.3501	0.3235	0.3459	0.3038	0.2833	0.3028	0.2584	0.2394	0.2555
0.25	0.4911	0.4668	0.4972		0.4100	0.4375		0.3455	0.3691
0.30	0.6464	0.6148	0.6488	0.5703	0.5473	0.5800	0.4918	0.4659	0.4957
0.35	0.7809	0.7476	0.7797	0.7112	0.6791	0.7126		0.5897	0.6228
0.40	0.8725	0.8514	0.8769	0.8235	0.7915	0.8211	0.7381	0.7051	0.7377
0.45	0.9370	0.9219	0.9392	0.8969	0.8766	0.8993		0.8027	0.8312
0.50	0.9770	0.9635	0.9735	0.9484	0.9338	0.9490	0.9019	0.8778	0.9000
0.55	0.9919	0.9849	0.9899	0.9791	0.9679	0.9769	0.9450	0.9301	0.9456
0.60		0.9945	0.9966	0.9926	0.9860	0.9906	0.9755	0.9632	0.9729
0.65		0.9982	0.9990		0.9945	0.9966	0.9902	0.9822	0.9877
0.70		0.9995	0.9998		0.9981	0.9989	0.9964	0.9921	0.9949

sample size 500, a = -1

b	A = 0.2			A = 0.5			A = 0.8		
	simulation	formula population	formula sample	simulation	formula population	formula sample	simulation	formula population	formula sample
0.00	0.0493	0.0500	0.0500	0.0535	0.0500	0.0500	0.0509	0.0500	0.0500
0.05	0.0884	0.0912	0.0904	0.0803	0.0850	0.0843	0.0751	0.0784	0.0778
0.10	0.2131	0.2205	0.2172	0.1883	0.1948	0.1919	0.1611	0.1671	0.1648
0.15	0.4165	0.4287	0.4220	0.3677	0.3759	0.3699	0.3073	0.3165	0.3115
0.20	0.6572	0.6604	0.6521	0.5793	0.5914	0.5833	0.4994	0.5063	0.4988
0.25	0.8377	0.8430	0.8362	0.7722	0.7820	0.7742	0.6915	0.6948	0.6866
0.30	0.9395	0.9452	0.9414	0.9008	0.9077	0.9025	0.8307	0.8422	0.8354
0.35	0.9854	0.9859	0.9844	0.9690	0.9696	0.9670	0.9317	0.9329	0.9286
0.40	0.9977	0.9973	0.9970	0.9907	0.9923	0.9914	0.9750	0.9768	0.9747

**POWER: UNIFORM COVARIATE
EXPONENTIAL SURVIVAL TIMES**

sample size 100, a = 0

b	simulation	A = 0.2		A = 0.5			A = 0.8		
		formula population	formula sample	simulation	formula population	formula sample	simulation	formula population	formula sample
0.00	0.0513	0.0500	0.0500	0.0492	0.0500	0.0500	0.0472	0.0500	0.0500
0.05	0.0718	0.0671	0.0694	0.0682	0.0651	0.0671	0.0675	0.0626	0.0643
0.10	0.1282	0.1202	0.1295	0.1180	0.1117	0.1198	0.1068	0.1013	0.1080
0.15	0.2295	0.2113	0.2320	0.2092	0.1918	0.2100	0.1858	0.1678	0.1830
0.20	0.3641	0.3374	0.3716	0.3315	0.3039	0.3345		0.2620	0.2879
0.25	0.5305	0.4860	0.5308		0.4395	0.4809	0.4035	0.3790	0.4155
0.30	0.6860	0.6367	0.6849	0.6352	0.5828	0.6297		0.5088	0.5527
0.35	0.8129	0.7687	0.8118		0.7158	0.7609	0.6831	0.6377	0.6835
0.40	0.8980	0.8686	0.9009	0.8675	0.8243	0.8613		0.7526	0.7943
0.45	0.9544	0.9338	0.9543	0.9306	0.9021	0.9281	0.8828	0.8444	0.8779
0.50	0.9803	0.9706	0.9816	0.9688	0.9510	0.9669		0.9104	0.9340
0.55		0.9885	0.9935	0.9869	0.9781	0.9865	0.9696	0.9529	0.9677
0.60		0.9961	0.9980	0.9953	0.9913	0.9951	0.9866	0.9775	0.9856
0.65		0.9988	0.9995		0.9969	0.9984	0.9955	0.9902	0.9942
0.70		0.9997	0.9999		0.9990	0.9996	0.9976	0.9961	0.9979

sample size 200, a = 0

b	simulation	A = 0.2		A = 0.5			A = 0.8		
		formula population	formula sample	simulation	formula population	formula sample	simulation	formula population	formula sample
0.00	0.0530	0.0500	0.0500	0.0501	0.0500	0.0500	0.0518	0.0500	0.0500
0.05	0.0914	0.0846	0.0877	0.0844	0.0804	0.0831	0.0798	0.0753	0.0776
0.10	0.2062	0.1930	0.2057	0.1910	0.1757	0.1869	0.1624	0.1544	0.1637
0.15	0.3895	0.3721	0.3984	0.3525	0.3352	0.3589	0.3063	0.2886	0.3089
0.20	0.6148	0.5862	0.6212	0.5597	0.5339	0.5675	0.4806	0.4636	0.4945
0.25	0.8087	0.7770	0.8091	0.7598	0.7245	0.7585	0.6777	0.6464	0.6814
0.30	0.9257	0.9043	0.9251	0.8891	0.8659	0.8911	0.8227	0.8003	0.8306
0.35	0.9775	0.9679	0.9775	0.9576	0.9472	0.9610	0.9205	0.9049	0.9253
0.40	0.9939	0.9917	0.9949	0.9868	0.9834	0.9891	0.9712	0.9622	0.9729

sample size 500, a = 0

b	simulation	A = 0.2		A = 0.5			A = 0.8		
		formula population	formula sample	simulation	formula population	formula sample	simulation	formula population	formula sample
0.00	0.0497	0.0500	0.0500	0.0487	0.0500	0.0500	0.0445	0.0500	0.0500
0.05	0.1402	0.1382	0.1365	0.1241	0.1275	0.1260	0.1127	0.1145	0.1132
0.10	0.3986	0.4059	0.3994	0.3614	0.3658	0.3600	0.3076	0.3149	0.3099
0.15	0.7134	0.7331	0.7249	0.6596	0.6790	0.6706	0.5767	0.6010	0.5927
0.20	0.9259	0.9310	0.9265	0.8902	0.8985	0.8929	0.8293	0.8400	0.8330
0.25	0.9890	0.9905	0.9894	0.9780	0.9813	0.9795	0.9518	0.9585	0.9552
0.30	0.9992	0.9993	0.9992	0.9976	0.9981	0.9978	0.9922	0.9933	0.9924
0.35	1.0000	1.0000	1.0000	1.0000	0.9999	0.9999	0.9990	0.9993	0.9992
0.40	1.0000	1.0000	1.0000	0.9999	1.0000	1.0000	1.0000	1.0000	1.0000

**POWER: UNIFORM COVARIATE
EXPONENTIAL SURVIVAL TIMES**

sample size 100, a = 1

b	A = 0.2			A = 0.5			A = 0.8		
	simulation	formula population	formula sample	simulation	formula population	formula sample	simulation	formula population	formula sample
0.00	0.0501	0.0500	0.0500	0.0466	0.0500	0.0500	0.0490	0.0500	0.0500
0.05	0.0809	0.0765	0.0801	0.0786	0.0750	0.0783	0.0733	0.0721	0.0751
0.10	0.1721	0.1593	0.1742	0.1597	0.1528	0.1667	0.1500	0.1410	0.1533
0.15	0.3250	0.2994	0.3317	0.3087	0.2850	0.3154	0.2833	0.2586	0.2857
0.20	0.5131	0.4802	0.5284	0.4910	0.4580	0.5041	0.4479	0.4159	0.4584
0.25	0.7053	0.6656	0.7182	0.6744	0.6398	0.6919	0.6283	0.5887	0.6396
0.30	0.8498	0.8174	0.8607	0.8301	0.7943	0.8392	0.7823	0.7457	0.7934
0.35	0.9342	0.9167	0.9440	0.9209	0.9006	0.9307	0.8879	0.8639	0.8995
0.40	0.9760	0.9686	0.9819	0.9692	0.9598	0.9756	0.9518	0.9376	0.9589
0.45	0.9924	0.9903	0.9953	0.9905	0.9865	0.9930	0.9824	0.9757	0.9860

sample size 200, a = 1

b	A = 0.2			A = 0.5			A = 0.8		
	simulation	formula population	formula sample	simulation	formula population	formula sample	simulation	formula population	formula sample
0.00	0.0493	0.0500	0.0500	0.0487	0.0500	0.0500	0.0517	0.0500	0.0500
0.05	0.1080	0.1037	0.1085	0.1049	0.1005	0.1051	0.0944	0.0947	0.0988
0.10	0.2872	0.2717	0.2912	0.2754	0.2588	0.2772	0.2542	0.2351	0.2515
0.15	0.5575	0.5264	0.5609	0.5354	0.5027	0.5362	0.4921	0.4576	0.4890
0.20	0.8016	0.7708	0.8043	0.7772	0.7461	0.7805	0.7309	0.6954	0.7310
0.25	0.9354	0.9218	0.9407	0.9219	0.9062	0.9274	0.8914	0.8705	0.8960
0.30	0.9876	0.9818	0.9882	0.9831	0.9758	0.9838	0.9810	0.9597	0.9714
0.35	0.9978	0.9972	0.9985	0.9969	0.9957	0.9976	0.9929	0.9910	0.9945
0.40	0.9999	0.9997	0.9999	0.9996	0.9995	0.9998	0.9990	0.9986	0.9993

sample size 500, a = 1

b	A = 0.2			A = 0.5			A = 0.8		
	simulation	formula population	formula sample	simulation	formula population	formula sample	simulation	formula population	formula sample
0.00	0.0525	0.0500	0.0500	0.0515	0.0500	0.0500	0.0505	0.0500	0.0500
0.05	0.1859	0.1874	0.1847	0.1818	0.1793	0.1767	0.1648	0.1644	0.1621
0.10	0.5611	0.5698	0.5616	0.5366	0.5451	0.5370	0.4865	0.4975	0.4899
0.15	0.8836	0.8932	0.8873	0.8664	0.8749	0.8685	0.8262	0.8341	0.8269
0.20	0.9874	0.9896	0.9884	0.9828	0.9856	0.9841	0.9716	0.9743	0.9719
0.25	0.9995	0.9996	0.9996	0.9994	0.9994	0.9992	0.9979	0.9983	0.9980
0.30	1.0000	1.0000	1.0000	0.9999	1.0000	1.0000	0.9999	1.0000	0.9999

**POWER: GAMMA(3) COVARIATE
EXPONENTIAL SURVIVAL TIMES**

sample size 100, a = -1

b	A = 0.2			A = 0.5			A = 0.8		
	simulation	formula population	formula sample	simulation	formula population	formula sample	simulation	formula population	formula sample
0.00	0.0509	0.0500	0.0500	0.0473	0.0500	0.0500	0.0484	0.0500	0.0500
0.05	0.0674	0.0581	0.0594	0.0640	0.0569	0.0580	0.0614	0.0556	0.0565
0.10	0.1040	0.0828	0.0880	0.0975	0.0779	0.0823	0.0885	0.0726	0.0762
0.15	0.1684	0.1252	0.1370	0.1534	0.1138	0.1238		0.1016	0.1097
0.20	0.2516	0.1857	0.2069		0.1652	0.1831	0.1961	0.1431	0.1576
0.25		0.2638	0.2960	0.3138	0.2319	0.2595		0.1972	0.2198
0.30	0.4780	0.3567	0.4000		0.3123	0.3503	0.3642	0.2633	0.2950
0.35		0.4593	0.5117	0.5528	0.4033	0.4508		0.3397	0.3805
0.40	0.7442	0.5648	0.6224		0.5000	0.5544	0.5868	0.4236	0.4723
0.45		0.6658	0.7237	0.7915	0.5967	0.6543		0.5112	0.5656
0.50	0.9135	0.7561	0.8093		0.6878	0.7444	0.8084	0.5983	0.6552
0.55	0.9577	0.8313	0.8763	0.9289	0.7687	0.8203		0.6807	0.7367
0.60	0.9814	0.8896	0.9247	0.9640	0.8364	0.8801	0.9317	0.7551	0.8070
0.65	0.9930	0.9319	0.9571	0.9844	0.8896	0.9242	0.9649	0.8190	0.8643
0.70	0.9988	0.9604	0.9771	0.9951	0.9292	0.9547	0.9810	0.8713	0.9087
0.75		0.9783	0.9886	0.9988	0.9568	0.9744	0.9932	0.9120	0.9412
0.80		0.9889	0.9947		0.9750	0.9864	0.9977	0.9423	0.9638

sample size 200, a = -1

b	A = 0.2			A = 0.5			A = 0.8		
	simulation	formula population	formula sample	simulation	formula population	formula sample	simulation	formula population	formula sample
0.00	0.0489	0.0500	0.0500	0.0481	0.0500	0.0500	0.0484	0.0500	0.0500
0.05	0.0680	0.0663	0.0661	0.0682	0.0639	0.0637	0.0626	0.0612	0.0611
0.10	0.1304	0.1166	0.1156	0.1150	0.1065	0.1057	0.1024	0.0958	0.0951
0.15	0.3749	0.2031	0.2007		0.1800	0.1779		0.1551	0.1534
0.20		0.3235	0.3191	0.3323	0.2833	0.2795	0.2855	0.2394	0.2362
0.25	0.5154	0.4668	0.4603		0.4100	0.4041		0.3455	0.3404
0.30	0.6770	0.6148	0.6068	0.6066	0.5473	0.5395	0.5285	0.4659	0.4589
0.35	0.8098	0.7476	0.7393	0.7481	0.6791	0.6704		0.5897	0.5811
0.40	0.8933	0.8514	0.8440	0.8569	0.7915	0.7830	0.7820	0.7051	0.6959
0.45	0.9524	0.9219	0.9163	0.9233	0.8766	0.8694		0.8027	0.7939
0.50	0.9846	0.9635	0.9599	0.9646	0.9338	0.9284	0.9343	0.8778	0.8701
0.55	0.9955	0.9849	0.9829	0.9879	0.9679	0.9644	0.9708	0.9301	0.9242
0.60		0.9945	0.9936	0.9963	0.9860	0.9840	0.9876	0.9632	0.9591
0.65		0.9982	0.9978		0.9945	0.9935	0.9964	0.9822	0.9796
0.70		0.9995	0.9994		0.9981	0.9976	0.9991	0.9921	0.9907

sample size 500, a = -1

b	A = 0.2			A = 0.5			A = 0.8		
	simulation	formula population	formula sample	simulation	formula population	formula sample	simulation	formula population	formula sample
0.00	0.0511	0.0500	0.0500	0.0549	0.0500	0.0500	0.0528	0.0500	0.0500
0.05	0.0872	0.0912	0.0869	0.0848	0.0850	0.0813	0.0779	0.0784	0.0754
0.10	0.2195	0.2205	0.2025	0.1976	0.1948	0.1794	0.1688	0.1671	0.1546
0.15	0.4270	0.4287	0.3917	0.3762	0.3759	0.3430	0.3231	0.3165	0.2889
0.20	0.6696	0.6604	0.6125	0.5990	0.5914	0.5450	0.5204	0.5063	0.4639
0.25	0.8513	0.8430	0.8013	0.7945	0.7820	0.7358	0.7169	0.6948	0.6464
0.30	0.9489	0.9452	0.9202	0.9197	0.9077	0.8744	0.8636	0.8422	0.8001
0.35	0.9900	0.9859	0.9754	0.9783	0.9696	0.9520	0.9509	0.9329	0.9045
0.40	0.9985	0.9973	0.9942	0.9946	0.9923	0.9854	0.9829	0.9768	0.9619

**POWER: GAMMA(3) COVARIATE
EXPONENTIAL SURVIVAL TIMES**

sample size 100, a = 0

b	simulation	A = 0.2		A = 0.5			A = 0.8		
		formula population	formula sample	simulation	formula population	formula sample	simulation	formula population	formula sample
0.00	0.0479	0.0500	0.0500	0.0489	0.0500	0.0500	0.0490	0.0500	0.0500
0.05	0.0793	0.0671	0.0699	0.0758	0.0651	0.0675	0.0743	0.0626	0.0646
0.10	0.1496	0.1202	0.1314	0.1371	0.1117	0.1216	0.1275	0.1013	0.1095
0.15	0.2636	0.2113	0.2368	0.2416	0.1918	0.2143	0.2178	0.1678	0.1866
0.20	0.4127	0.3374	0.3799	0.3824	0.3039	0.3422		0.2620	0.2945
0.25	0.5929	0.4860	0.5424		0.4395	0.4921	0.4786	0.3790	0.4257
0.30	0.7596	0.6367	0.6979	0.7049	0.5828	0.6430		0.5088	0.5657
0.35	0.8704	0.7687	0.8237		0.7158	0.7742	0.7663	0.6377	0.6978
0.40	0.9411	0.8686	0.9100	0.9204	0.8243	0.8725		0.7526	0.8080
0.45	0.9785	0.9338	0.9600	0.9662	0.9021	0.9362	0.9379	0.8444	0.8892
0.50	0.9916	0.9706	0.9847	0.9878	0.9510	0.9718		0.9104	0.9422
0.55		0.9885	0.9949	0.9965	0.9781	0.9891	0.9925	0.9529	0.9728
0.60		0.9961	0.9986	0.9986	0.9913	0.9963	0.9966	0.9775	0.9885
0.65		0.9988	0.9996		0.9969	0.9989	0.9993	0.9902	0.9957
0.70		0.9997	0.9999		0.9990	0.9997	0.9998	0.9961	0.9985

sample size 200, a = 0

b	simulation	A = 0.2		A = 0.5			A = 0.8		
		formula population	formula sample	simulation	formula population	formula sample	simulation	formula population	formula sample
0.00	0.0541	0.0500	0.0500	0.0523	0.0500	0.0500	0.0521	0.0500	0.0500
0.05	0.0910	0.0846	0.0841	0.0867	0.0804	0.0800	0.0825	0.0753	0.0750
0.10	0.2068	0.1930	0.1910	0.1924	0.1757	0.1739	0.1717	0.1544	0.1529
0.15	0.3888	0.3721	0.3676	0.3528	0.3352	0.3311	0.3071	0.2886	0.2851
0.20	0.6143	0.5862	0.5797	0.5626	0.5339	0.5276	0.4894	0.4636	0.4578
0.25	0.8059	0.7770	0.7704	0.7546	0.7245	0.7174	0.6792	0.6464	0.6392
0.30	0.9240	0.9043	0.8995	0.8871	0.8659	0.8601	0.8331	0.8003	0.7934
0.35	0.9776	0.9679	0.9654	0.9606	0.9472	0.9436	0.9269	0.9049	0.8997
0.40	0.9928	0.9917	0.9907	0.9879	0.9834	0.9817	0.9728	0.9622	0.9591

sample size 500, a = 0

b	simulation	A = 0.2		A = 0.5			A = 0.8		
		formula population	formula sample	simulation	formula population	formula sample	simulation	formula population	formula sample
0.00	0.0480	0.0500	0.0500	0.0486	0.0500	0.0500	0.0454	0.0500	0.0500
0.05	0.1373	0.1382	0.1289	0.1271	0.1275	0.1194	0.1158	0.1145	0.1077
0.10	0.3860	0.4059	0.3709	0.3552	0.3658	0.3341	0.3068	0.3149	0.2877
0.15	0.7047	0.7331	0.6860	0.6571	0.6790	0.6314	0.5761	0.6010	0.5547
0.20	0.9186	0.9310	0.9030	0.8887	0.8985	0.8643	0.8286	0.8400	0.7984
0.25	0.9878	0.9905	0.9827	0.9768	0.9813	0.9688	0.9541	0.9585	0.9375
0.30	0.9993	0.9993	0.9983	0.9977	0.9981	0.9957	0.9932	0.9933	0.9872
0.35	1.0000	1.0000	0.9999	0.9998	0.9999	0.9997	0.9994	0.9993	0.9983

**POWER: GAMMA(3) COVARIATE
EXPONENTIAL SURVIVAL TIMES**

sample size 100

b	a = -1, A = 0.8			a = 0, A = 0.5			a = 1, A = 0.2		
	simulation	formula population	formula sample	simulation	formula population	formula sample	simulation	formula population	formula sample
0.00	0.0484	0.0500	0.0500	0.0489	0.0500	0.0500	0.0505	0.0500	0.0500
-0.05	0.0416	0.0556	0.0565	0.0581	0.0651	0.0675	0.0735	0.0765	0.0808
-0.10	0.0513	0.0726	0.0764	0.0999	0.1117	0.1219	0.1576	0.1593	0.1772
-0.15		0.1016	0.1103	0.1749	0.1918	0.2155	0.3092	0.2994	0.3387
-0.20	0.0969	0.1431	0.1590	0.2787	0.3039	0.3449	0.4892	0.4802	0.5391
-0.25		0.1972	0.2225		0.4395	0.4966	0.6773	0.6656	0.7301
-0.30	0.1981	0.2633	0.2996	0.5459	0.5828	0.6492	0.8178	0.8174	0.8704
-0.35		0.3397	0.3874		0.7158	0.7809	0.9161	0.9167	0.9499
-0.40	0.3284	0.4236	0.4818	0.7903	0.8243	0.8786	0.9648	0.9686	0.9846
-0.45		0.5112	0.5774	0.8794	0.9021	0.9407	0.9883	0.9903	0.9963
-0.50	0.4744	0.5983	0.6688	0.9360	0.9510	0.9747		0.9976	0.9993
-0.55		0.6807	0.7512	0.9726	0.9781	0.9906		0.9995	0.9999
-0.60	0.6461	0.7551	0.8213	0.9844	0.9913	0.9970		0.9999	
-0.65	0.7214	0.8190	0.8776		0.9969	0.9991			
-0.70	0.7812	0.8713	0.9201		0.9990	0.9998			
-0.75	0.8443	0.9120	0.9504		0.9997				
-0.80	0.8878	0.9423	0.9708		0.9999				

sample size 200

b	a = -1, A = 0.8			a = 0, A = 0.5			a = 1, A = 0.2		
	simulation	formula population	formula sample	simulation	formula population	formula sample	simulation	formula population	formula sample
0.00	0.0484	0.0500	0.0500	0.0523	0.0500	0.0500	0.0496	0.0500	0.0500
-0.05	0.0543	0.0612	0.0611	0.0767	0.0804	0.0801	0.0963	0.1037	0.1030
-0.10	0.0812	0.0958	0.0953	0.1618	0.1757	0.1743	0.2548	0.2717	0.2691
-0.15		0.1551	0.1542	0.3093	0.3352	0.3326	0.4877	0.5264	0.5220
-0.20	0.1943	0.2394	0.2380	0.4858	0.5339	0.5304	0.7355	0.7708	0.7664
-0.25		0.3455	0.3437	0.6737	0.7245	0.7212	0.8992	0.9218	0.9191
-0.30	0.3910	0.4659	0.4640	0.8201	0.8659	0.8637	0.9700	0.9818	0.9809
-0.35		0.5897	0.5880	0.9172	0.9472	0.9461	0.9949	0.9972	0.9970
-0.40	0.6122	0.7051	0.7039	0.9685	0.9834	0.9830	0.9996	0.9997	0.9997
-0.45		0.8027	0.8021		0.9959	0.9958			
-0.50	0.8073	0.8778	0.8776		0.9992	0.9992			
-0.55	0.8766	0.9301	0.9302		0.9999	0.9999			
-0.60	0.9259	0.9632	0.9635						
-0.65	0.9616	0.9822	0.9825						
-0.70	0.9819	0.9921	0.9923						

sample size 500

b	a = -1, A = 0.8			a = 0, A = 0.5			a = 1, A = 0.2		
	simulation	formula population	formula sample	simulation	formula population	formula sample	simulation	formula population	formula sample
0.00	0.0528	0.0500	0.0500	0.0486	0.0500	0.0500	0.0509	0.0500	0.0500
-0.05	0.0666	0.0784	0.0754	0.1139	0.1275	0.1194	0.1666	0.1874	0.1730
-0.10	0.1343	0.1671	0.1549	0.3168	0.3658	0.3346	0.5102	0.5698	0.5254
-0.15	0.2515	0.3165	0.2898	0.6023	0.6790	0.6326	0.8476	0.8932	0.8589
-0.20	0.4092	0.5063	0.4658	0.8401	0.8985	0.8656	0.9772	0.9896	0.9816
-0.25	0.5877	0.6948	0.6492	0.9545	0.9813	0.9695	0.9982	0.9996	0.9990
-0.30	0.7395	0.8422	0.8031	0.9915	0.9981	0.9959	0.9999	1.0000	1.0000
-0.35	0.8617	0.9329	0.9070	0.9988	0.9999	0.9997	1.0000	1.0000	1.0000
-0.40	0.9339	0.9768	0.9635	0.9998	1.0000	1.0000	1.0000	1.0000	1.0000

**POWER: NORMAL COVARIATE
WEIBULL SURVIVAL TIMES**

sample size 200, A = 0.5

shape = 0.2, a = -1.25				shape = 0.2, a = -0.75			shape = 0.2, a = -0.25		
b	simulation	formula population	formula sample	simulation	formula population	formula sample	simulation	formula population	formula sample
0.00	0.0505	0.0500	0.0500	0.0547	0.0500	0.0500	0.0485	0.0500	0.0500
0.10	0.1099	0.1056	0.1125	0.1442	0.1354	0.1460	0.1872	0.1748	0.1904
0.20	0.2978	0.2797	0.3061	0.4189	0.3954	0.4326	0.5655	0.5312	0.5773
0.30	0.5693	0.5408	0.5847	0.7583	0.7195	0.7643	0.8842	0.8638	0.8974
0.40	0.817	0.7852	0.8244	0.9417	0.9234	0.9459	0.9893	0.9829	0.9902
0.50	0.9481	0.9302	0.9503	0.9934	0.9886	0.9936			
0.60	0.9911	0.9848	0.9909						

shape = 0.5, a = -1.15				shape = 0.5, a = -0.65			shape = 0.5, a = -0.15		
b	simulation	formula population	formula sample	simulation	formula population	formula sample	simulation	formula population	formula sample
0.00	0.0505	0.0500	0.0500	0.0547	0.0500	0.0500	0.0485	0.0500	0.0500
0.10	0.1099	0.1062	0.1131	0.1442	0.1361	0.1468	0.1872	0.1756	0.1913
0.20	0.2978	0.2819	0.3086	0.4189	0.3980	0.4355	0.5655	0.5337	0.5799
0.30	0.5693	0.5447	0.5887	0.7583	0.7230	0.7676	0.8842	0.8658	0.8992
0.40	0.817	0.7890	0.8280	0.9417	0.9254	0.9475	0.9893	0.9834	0.9906
0.50	0.9481	0.9324	0.9520	0.9934	0.9891	0.9939			
0.60	0.9911	0.9855	0.9914						

shape = 2, a = -0.75				shape = 2, a = -0.25			shape = 2, a = 0.25		
b	simulation	formula population	formula sample	simulation	formula population	formula sample	simulation	formula population	formula sample
0.00	0.0505	0.0500	0.0500	0.0547	0.0500	0.0500	0.0485	0.0500	0.0500
0.10	0.1099	0.1058	0.1127	0.1442	0.1347	0.1452	0.1872	0.1723	0.1875
0.20	0.2978	0.2802	0.3068	0.4189	0.3929	0.4300	0.5655	0.5231	0.5689
0.30	0.5693	0.5418	0.5857	0.7583	0.7163	0.7612	0.8842	0.8569	0.8916
0.40	0.817	0.7862	0.8254	0.9417	0.9216	0.9445	0.9893	0.9810	0.9891
0.50	0.9481	0.9308	0.9508	0.9934	0.9881	0.9933			
0.60	0.9911	0.9850	0.9910						

shape = 5, a = -0.1				shape = 5, a = 0.5			shape = 5, a = 1.1		
b	simulation	formula population	formula sample	simulation	formula population	formula sample	simulation	formula population	formula sample
0.00	0.0505	0.0500	0.0500	0.0547	0.0500	0.0500	0.0485	0.0500	0.0500
0.10	0.1099	0.1055	0.1123	0.1442	0.1367	0.1476	0.1872	0.1741	0.1897
0.20	0.2978	0.2790	0.3056	0.4189	0.4004	0.4385	0.5655	0.5290	0.5756
0.30	0.5693	0.5396	0.5839	0.7583	0.7261	0.7713	0.8842	0.8619	0.8966
0.40	0.817	0.7840	0.8239	0.9417	0.9271	0.9494	0.9893	0.9824	0.9901
0.50	0.9481	0.9295	0.9501	0.9934	0.9895	0.9943			
0.60	0.9911	0.9846	0.9908						

**POWER: UNIFORM COVARIATE
WEIBULL SURVIVAL TIMES
sample size 200, A = 0.5**

b	shape = 0.2, a = -1.25			shape = 0.2, a = -0.75			shape = 0.2, a = -0.25		
	simulation	formula population	formula sample	simulation	formula population	formula sample	simulation	formula population	formula sample
0.00	0.0479	0.0500	0.0500	0.0518	0.0500	0.0500	0.0489	0.0500	0.0500
0.10	0.1069	0.1056	0.1106	0.1427	0.1354	0.1430	0.1817	0.1748	0.1860
0.20	0.2949	0.2797	0.2989	0.4156	0.3954	0.4225	0.5638	0.5312	0.5648
0.30	0.5706	0.5408	0.5734	0.753	0.7195	0.7530	0.8805	0.8638	0.8892
0.40	0.8138	0.7852	0.8151	0.9418	0.9234	0.9408	0.9896	0.9829	0.9887
0.50	0.9498	0.9302	0.9460	0.9927	0.9886	0.9926			
0.60	0.9922	0.9848	0.9897						

b	shape = 0.5, a = -1.15			shape = 0.5, a = -0.65			shape = 0.5, a = -0.15		
	simulation	formula population	formula sample	simulation	formula population	formula sample	simulation	formula population	formula sample
0.00	0.0494	0.0500	0.0500	0.0495	0.0500	0.0500	0.0495	0.0500	0.0500
0.10	0.1089	0.1062	0.1112	0.1452	0.1361	0.1438	0.184	0.1756	0.1868
0.20	0.2966	0.2819	0.3013	0.4222	0.3980	0.4253	0.5636	0.5337	0.5674
0.30	0.5734	0.5447	0.5774	0.7584	0.7230	0.7563	0.8833	0.8658	0.8910
0.40	0.8177	0.7890	0.8187	0.9427	0.9254	0.9425	0.9903	0.9834	0.9891
0.50	0.95	0.9324	0.9478	0.9928	0.9891	0.9930			
0.60	0.9921	0.9855	0.9903						

b	shape = 2, a = -0.75			shape = 2, a = -0.25			shape = 2, a = 0.25		
	simulation	formula population	formula sample	simulation	formula population	formula sample	simulation	formula population	formula sample
0.00	0.0479	0.0500	0.0500	0.051	0.0500	0.0500	0.0537	0.0500	0.0500
0.10	0.1068	0.1058	0.1107	0.135	0.1347	0.1423	0.18	0.1723	0.1832
0.20	0.2882	0.2802	0.2995	0.4099	0.3929	0.4199	0.55	0.5231	0.5564
0.30	0.5799	0.5418	0.5744	0.7409	0.7163	0.7498	0.8806	0.8569	0.8830
0.40	0.819	0.7862	0.8161	0.936	0.9216	0.9393	0.9862	0.9810	0.9874
0.50	0.9466	0.9308	0.9465	0.992	0.9881	0.9923			
0.60	0.9919	0.9850	0.9899						

b	shape = 5, a = -0.1			shape = 5, a = 0.5			shape = 5, a = 1.1		
	simulation	formula population	formula sample	simulation	formula population	formula sample	simulation	formula population	formula sample
0.00	0.0497	0.0500	0.0500	0.051	0.0500	0.0500	0.053	0.0500	0.0500
0.10	0.1107	0.1055	0.1104	0.1413	0.1367	0.1445	0.1807	0.1741	0.1853
0.20	0.289	0.2790	0.2983	0.413	0.4004	0.4280	0.5523	0.5290	0.5629
0.30	0.5661	0.5396	0.5724	0.7366	0.7261	0.7597	0.88	0.8619	0.8879
0.40	0.8113	0.7840	0.8143	0.9369	0.9271	0.9442	0.9853	0.9824	0.9884
0.50	0.9445	0.9295	0.9456	0.9923	0.9895	0.9933			
0.60	0.9886	0.9846	0.9896						

**POWER: GAMMA(3) COVARIATE
WEIBULL SURVIVAL TIMES
sample size 200, A = 0.5**

b	shape = 0.2, a = -1.25			shape = 0.2, a = -0.75			shape = 0.2, a = -0.25		
	simulation	formula population	formula sample	simulation	formula population	formula sample	simulation	formula population	formula sample
0.00	0.0525	0.0500	0.0500	0.0531	0.0500	0.0500	0.0491	0.0500	0.0500
0.10	0.1195	0.1056	0.1048	0.1535	0.1354	0.1342	0.185	0.1748	0.1731
0.20	0.32	0.2797	0.2759	0.4346	0.3954	0.3901	0.5637	0.5312	0.5249
0.30	0.6068	0.5408	0.5331	0.7735	0.7195	0.7117	0.8866	0.8638	0.8579
0.40	0.8524	0.7852	0.7766	0.9518	0.9234	0.9184	0.9907	0.9829	0.9811
0.50	0.9684	0.9302	0.9247	0.9955	0.9886	0.9871			
0.60	0.9968	0.9848	0.9827						

b	shape = 0.5, a = -1.15			shape = 0.5, a = -0.65			shape = 0.5, a = -0.15		
	simulation	formula population	formula sample	simulation	formula population	formula sample	simulation	formula population	formula sample
0.00	0.0504	0.0500	0.0500	0.0505	0.0500	0.0500	0.0481	0.0500	0.0500
0.10	0.1211	0.1062	0.1054	0.1554	0.1361	0.1349	0.19	0.1756	0.1739
0.20	0.3226	0.2819	0.2781	0.4357	0.3980	0.3927	0.5656	0.5337	0.5274
0.30	0.6076	0.5447	0.5370	0.773	0.7230	0.7151	0.8875	0.8658	0.8600
0.40	0.8569	0.7890	0.7805	0.9535	0.9254	0.9204	0.9906	0.9834	0.9817
0.50	0.9674	0.9324	0.9269	0.995	0.9891	0.9876			
0.60	0.9962	0.9855	0.9835						

b	shape = 2, a = -0.75			shape = 2, a = -0.25			shape = 2, a = 0.25		
	simulation	formula population	formula sample	simulation	formula population	formula sample	simulation	formula population	formula sample
0.00	0.0502	0.0500	0.0500	0.0493	0.0500	0.0500	0.0545	0.0500	0.0500
0.10	0.1158	0.1058	0.1050	0.1428	0.1347	0.1335	0.1807	0.1723	0.1706
0.20	0.3089	0.2802	0.2764	0.4249	0.3929	0.3877	0.5499	0.5231	0.5169
0.30	0.6114	0.5418	0.5341	0.7569	0.7163	0.7085	0.8767	0.8569	0.8510
0.40	0.8519	0.7862	0.7777	0.9466	0.9216	0.9165	0.9882	0.9810	0.9792
0.50	0.9645	0.9308	0.9253	0.9937	0.9881	0.9865			
0.60	0.995	0.9850	0.9829						

b	shape = 5, a = -0.1			shape = 5, a = 0.5			shape = 5, a = 1.1		
	simulation	formula population	formula sample	simulation	formula population	formula sample	simulation	formula population	formula sample
0.00	0.0509	0.0500	0.0500	0.0527	0.0500	0.0500	0.0534	0.0500	0.0500
0.10	0.1161	0.1055	0.1047	0.1421	0.1367	0.1355	0.1792	0.1741	0.1724
0.20	0.302	0.2790	0.2753	0.4278	0.4004	0.3953	0.5403	0.5290	0.5231
0.30	0.5933	0.5396	0.5322	0.7419	0.7261	0.7187	0.8762	0.8619	0.8565
0.40	0.84	0.7840	0.7758	0.9411	0.9271	0.9225	0.9849	0.9824	0.9808
0.50	0.9578	0.9295	0.9242	0.9928	0.9895	0.9882			
0.60	0.9937	0.9846	0.9825						