Linear regression, collinerarity, splines and extensions

Morten Frydenberg ©

Department of Biostatisics, Aarhus Univ, Denmark

General things for regression models:

Collinearity - correlated explanatory variables

Flexible modelling af response curves - Cubic splines

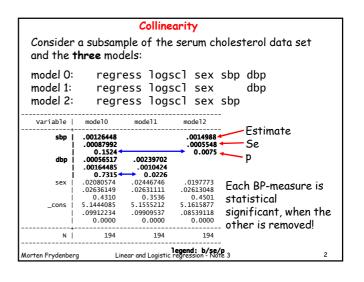
Normal regression models - extensions

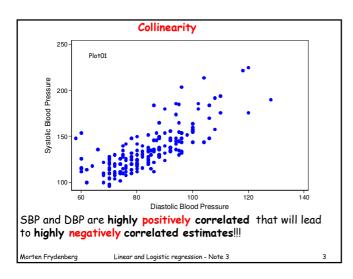
Random coefficient model

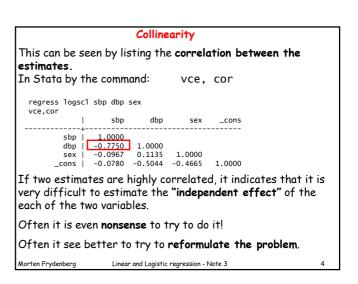
Clustered data / data with several random components

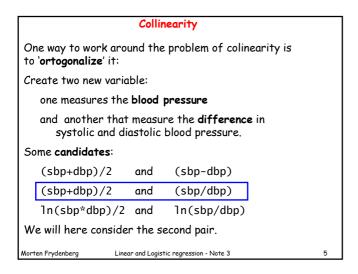
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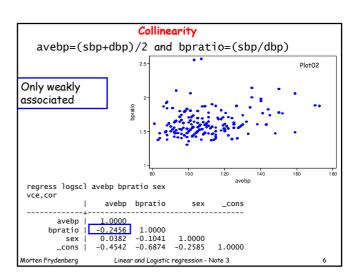
Linear and Logistic regression - Note 3

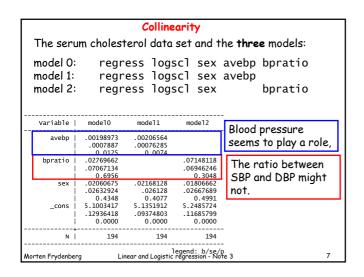








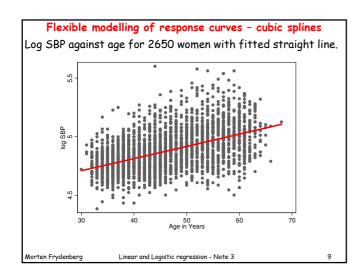


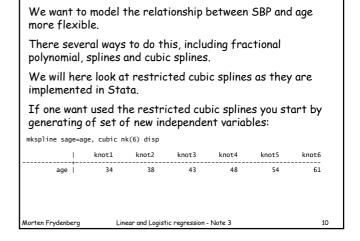


Collinearity Look out for it: •systolic and diastolic blood pressure •24 hour blood pressure and 'clinical' blood pressure •weight and height •age and parity •age and time since menopause •BMI and skinfold measure •age , birth cohort and calendar time •volume and concentration •...... Remember you will need a huge amount of data to disentangle

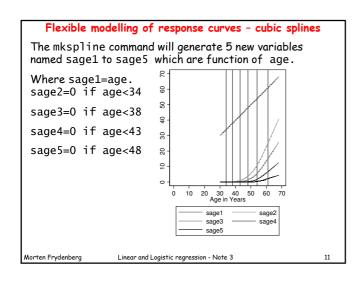
the effects of correlated explanatory variables

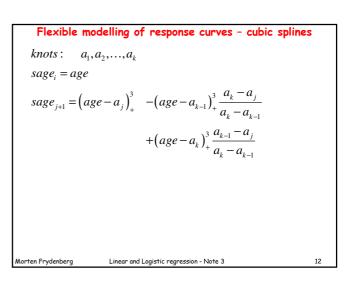
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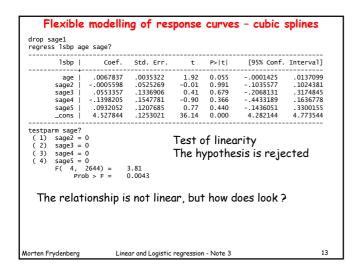


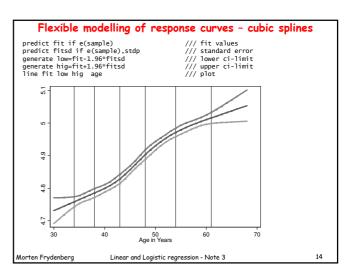


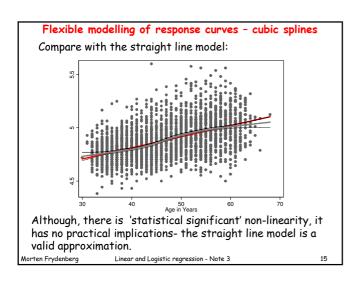
Flexible modelling of response curves - cubic splines

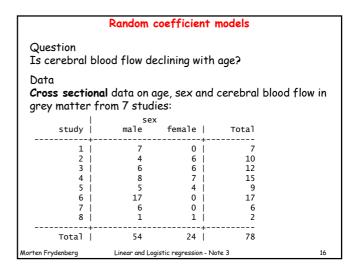


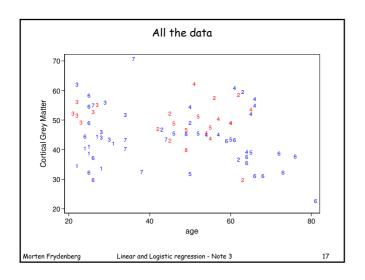


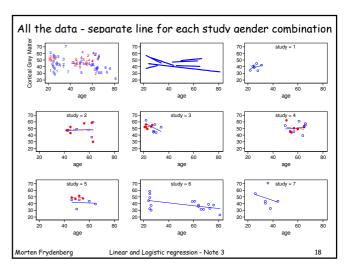


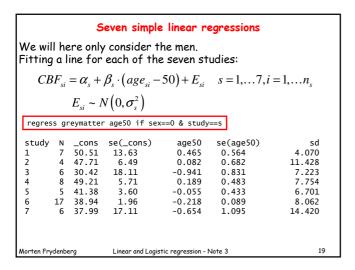


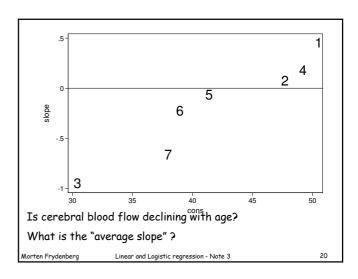


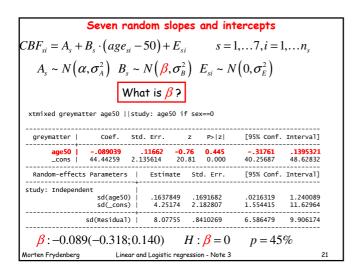


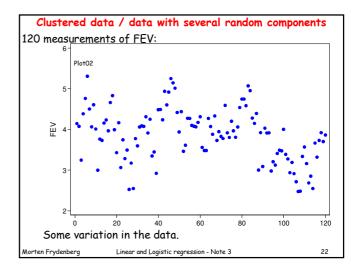


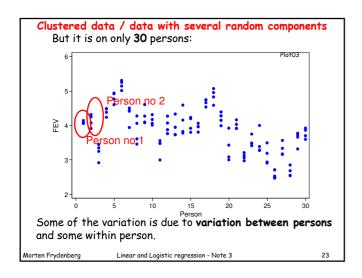


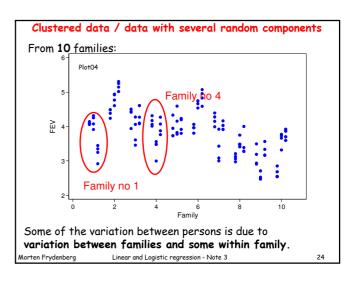














Structure of the data: FEV_{fpd}

Three sources of random variation:

Variation between families

Variation between persons (variation within family)

Variation between days (variation within person)

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near and Logistic regression - Note 3

Clustered data / data with several random components

Factors of interest:

household Income Constant within family
Urbanization Constant within family

Age Constant within person; varies within family

Sex Constant within person; varies within family

Grass pollen Constant within day; varies within person

A model:

 $FEV = \beta_0 + \beta_I \cdot I + \beta_U \cdot U + \beta_A \cdot A + \beta_S \cdot S + \beta_G \cdot G$

+random variation

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Clustered data / data with several random components

 $FEV = \beta_0 + \beta_I \cdot I + \beta_U \cdot U + \beta_A \cdot A + \beta_S \cdot S + \beta_G \cdot G$

+random variation

If the **three** levels/sources of **random** variation **are not** taken into account :

- · The precision of the β_I and β_U are highly overestimated
- The precision of the β_A and β_S are overestimated
- The estimates of the β_I and β_U will be biased if the not all families are represented by the same number of persons and each person is measured the same number of times.
- The estimates of the β_A and β_S will be biased if the not all persons are measured the same number of times.

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 $FEV = \beta_0 + \beta_I \cdot I + \beta_U \cdot U + \beta_A \cdot A + \beta_S \cdot S + \beta_G \cdot G$ $+ F_f + P_{fp} + E_{fpd}$

variance

Random family contribution σ_F^2 : Random person contribution σ_P^2

Random day contribution σ_E^2

 $var(FEV_{fpd}) = \sigma_F^2 + \sigma_P^2 + \sigma_E^2$ Variance components

Assumed to be normal distributed

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Clustered data / data with several random components
Systematic part

 $FEV = \frac{\beta_0 + \beta_I \cdot I + \beta_U \cdot U + \beta_A \cdot A + \beta_S \cdot S + \beta_G \cdot G}{+ \frac{F_f + P_{fp} + E_{fpa}}{Random part}}$ Random part

 $m{eta}_0, m{eta}_I, m{eta}_U, m{eta}_A, m{eta}_S$ and $m{eta}_G$ Quantify the **systematic** variation

 σ_F^2, σ_P^2 and σ_F^2

Quantify the random variation

This is a:

- ·Variance component model
- ·Mixed model (both systematic and random variation)
- ·Multilevel model

The theory behind and the understanding of such models is well established!!!

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