

PhD course in Basic Biostatistics - Day 7

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Post term delivery and parity
A two by two table

Odds and odds ratios

- Odds ratio and the relative risk
- Estimating the odds ratio
- Relative measures - why inference on the log-scale?
- Odds ratios, Confidence Intervals and testing

Odds ratio and logistic regression

Post term delivery and age of the woman

- A simple logistic regression model
- Understanding the model and the parameters
- The estimates
- Formulations

The risk versus age curves

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Post term delivery and parity - adjusting for age

Two simple logistic regression models
Comparing the slopes

A logistic regression model with the same slope
Understanding the parameters
The estimates
Formulation
A risk versus age and parity plot

Why use logistic regression

Linear and logistic regression models - a comparison

Why do we need regression models
Adjustment
Effect modification
Prediction

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Example: Post term delivery and parity

Question: How does the risk of post term delivery depend on parity?

Data: Parity and gestational age for 12,311 women in the age of 20 to 39. Post term delivery defined as a gestational age larger than 40 weeks.

| Parity | N | Postterm | Risk |
|-----------------|--------|----------|--------------------|
| First child | 5,938 | 1,722 | 29.0 (28.8; 30.2)% |
| Not first child | 6,373 | 1,677 | 26.3 (25.2; 27.4)% |
| Total | 12,311 | 3,399 | 27.6 (26.8; 28.4)% |

Model: Independent samples from two binomial distributions.

Let π_0 and π_1 be the probability (risk) of post term delivery among women giving birth to their first child or not, respectively.

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Example: Post term delivery and parity

The assumptions behind the model was discussed on day 4.

On that day we also looked at three different measures of associations: Risk Difference, Relative Risk and Odds Ratio. And the chi-squared test for no association.

Today we will look closer at the Odds Ratio.

| | |
|------------------------|--------------------|
| Risk difference | -2.7 (-4.3; -1.1)% |
| Relative risk | 0.91 (0.86; 0.96) |
| Odds ratio | 0.87 (0.81; 0.95) |
| $\chi^2=11.09$ p=0.001 | |

In the table above we compare π_1 to π_0 , i.e. women giving birth to their first child is the reference group.

We see that the risk is (statistically significant) smaller if the woman already had a child.

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Odds and risk

The **odds** is defined as $\pi/(1-\pi)$, i.e. the probability of post term delivery divided by the probability of not having a post term delivery.

$$\text{odds} = \frac{\pi}{1-\pi}$$

If the odds is equal to 0.5=1/2, then the risk of post term delivery is only **half** of the risk of not having a post term delivery.

We can also go from odds to risk:

$$\pi = \frac{\text{odds}}{1+\text{odds}}$$

We see that

$$\text{odds} = 0.5 \quad \text{gives} \quad \pi = 0.5/(1+0.5)=0.3333.$$

$$\text{odds} = 1 \quad \text{gives} \quad \pi = 1/(1+1)=0.5.$$

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Odds ratios and relative risks

The odds ratio is related to the relative risk:

$$OR_{10} = \frac{\pi_1 \cdot (1-\pi_0)}{\pi_0 \cdot (1-\pi_1)} = RR_{10} \cdot \frac{(1-\pi_0)}{(1-\pi_1)}$$

We can see that if the **event is rare**, i.e. both π_1 and π_0 are small, then the last ratio is close to 1/1=1.

So for a **rare event** we have:

$$OR \approx RR$$

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Odds and odds ratios

The odds ratio comparing parity>0 to the reference is given by

$$OR_{10} = \frac{\text{odds}_1}{\text{odds}_0} = \frac{\pi_1/(1-\pi_1)}{\pi_0/(1-\pi_0)} = \frac{\pi_1 \cdot (1-\pi_0)}{\pi_0 \cdot (1-\pi_1)}$$

It is easily seen that $\pi_1 = \pi_0 \Leftrightarrow \text{odds}_1 = \text{odds}_0 \Leftrightarrow OR = 1$

OR has **nice properties**:

Switching reference group or event will just lead to 1/OR, e.g.

$$OR_{01} = \frac{\text{odds}_0}{\text{odds}_1} = \frac{1}{OR_{10}}$$

And of course the estimates and confidence intervals will transform similarly.

$$OR_{01} : \frac{1}{0.87} \left(\frac{1}{0.95}; \frac{1}{0.81} \right) = 1.14 (1.06; 1.24)$$

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Estimating the odds ratios

The odds ratio is of course estimated by:

$$\widehat{OR}_{10} = \frac{\widehat{\pi}_1 \cdot (1-\widehat{\pi}_0)}{\widehat{\pi}_0 \cdot (1-\widehat{\pi}_1)}$$

Another way to find the estimate is to make the 'classical' 2x2 table:

| Exposed | Event | |
|---------|-------|----|
| | Yes | No |
| Yes | a | b |
| No | c | d |

$$\widehat{OR}_{10} = \frac{a \cdot d}{b \cdot c}$$

| Parity>0 | Post term | |
|----------|-----------|-------|
| | Yes | No |
| Yes | 1,677 | 4,696 |
| No | 1,722 | 4,216 |

$$\widehat{OR}_{10} = \frac{1,677 \cdot 4,216}{1,722 \cdot 4,696} = 0.8743$$

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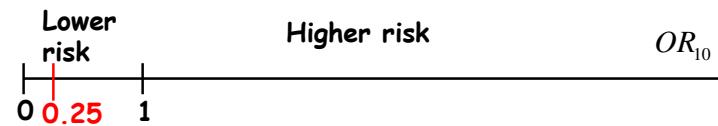
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Odds ratios - why inference on the log-scale

The odds ratio is limited to be positive.

A value in the interval **0 to 1** corresponds to lower risk among the Parity>0.

A value from **1 to infinity** corresponds to higher risk among the Parity>0



If we switch "exposed" and "unexposed" we get



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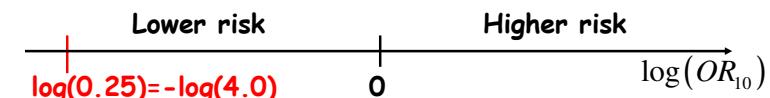
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Odds ratios - why inference on the log-scale

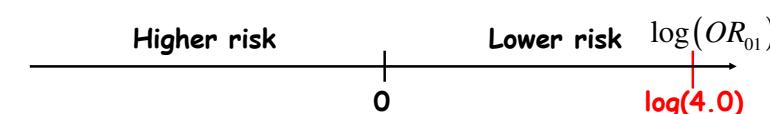
The **log-odds ratio** is not limited.

A value in the interval **-infinity to 0** corresponds to lower risk among the Parity>0.

A value from **0 to infinity** corresponds to higher risk among the Parity>0



If we switch "exposed" and "unexposed" we get



Symmetry on the log scale!!!

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Odds ratios - Approx. CI (Woolf/Wald)

So on the **log scale** we have a symmetric measure of association.

On the **log scale** it makes sense to find the CI as 'usual', i.e. as **estimate $\pm 1.96 \cdot se$** .

Using the notation from page 8 we have:

$$se(\ln(\widehat{OR})) = \sqrt{\frac{1}{a} + \frac{1}{b} + \frac{1}{c} + \frac{1}{d}}$$

$$se(\ln(\widehat{OR})) = \sqrt{\frac{1}{1,677} + \frac{1}{4,696} + \frac{1}{1,711} + \frac{1}{4,216}} = 0.0403$$

$$CI \ln(OR) = \ln(0.8743) \pm 1.96 \cdot 0.0403 = (-0.2134; -0.0552)$$

$$CI OR = (\exp(-0.2134); \exp(-0.0552)) = (0.81; 0.95)$$

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Odds ratios - Testing

If one wants to test a hypothesis that the odds ratio has a specific value: $OR = OR_0$,

then this is also done on the log-scale:

$$z_{obs} = \frac{\ln(\widehat{OR}) - \ln(OR_0)}{se(\ln(\widehat{OR}))}$$

Could the odds be reduced by 10%, i.e. H: $OR=0.9$?

$$z_{obs} = \frac{\ln(0.8743) - \ln(0.9)}{0.0403} = -0.719$$

$$p = 2 \cdot \Pr(z > |z_{obs}|) = 2 \cdot \Pr(z < -|z_{obs}|) = 0.47$$

The hypothesis cannot be rejected.

```
disp ( ln(0.8743)-ln(0.9) ) / 0.0403
disp 2*normal( abs(-0.719) )
```

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Odds ratios - logistic regression

Here we will see how one can find the odds ratio by **logistic regression**.

Let **Par1** be an **indicator variable** for Parity>0 , i.e. **Par1**=1 if parity>0 and **Par1**=0 if Parity==0.

Now we will look at the (logistic regression) model:

$$\log(\text{odds}) = \beta_0 + \beta_1 \cdot \text{Par1}$$

This is equivalent to:

$$\text{odds} = \exp(\beta_0 + \beta_1 \cdot \text{Par1}) = \exp(\beta_0) \cdot \exp(\beta_1)^{\text{Par1}}$$

and

$$\pi = \frac{\exp(\beta_0 + \beta_1 \cdot \text{Par1})}{1 + \exp(\beta_0 + \beta_1 \cdot \text{Par1})}$$

Odds ratios - logistic regression

$$\log(\text{odds}) = \beta_0 + \beta_1 \cdot \text{Par1} \quad \text{odds} = \exp(\beta_0) \cdot \exp(\beta_1)^{\text{Par1}}$$

In summary we have that in the model:

The "intercept" β_0 is the log odds in the "reference group".

The "slope" β_1 is the log OR.

That is, we can find the odds ratio from before by what is called a **logistic regression model**.

So the computer will give us **estimates and confidence intervals** for the **odds in the reference group** and the **odds ratio** comparing the 'exposed' to the reference.

Odds ratios - logistic regression

$$\log(\text{odds}) = \beta_0 + \beta_1 \cdot \text{Par1} \quad \text{odds} = \exp(\beta_0) \cdot \exp(\beta_1)^{\text{Par1}}$$

We see that if **Parity=0** then we have:

$$\log(\text{odds}) = \beta_0 \quad \text{odds} = \exp(\beta_0)$$

and if **Parity>0** then we have

$$\log(\text{odds}) = \beta_0 + \beta_1 \quad \text{odds} = \exp(\beta_0) \cdot \exp(\beta_1)$$

Combining we have

$$OR_{10} = \frac{\text{odds}(if\ parity > 0)}{\text{odds}(if\ parity == 0)} = \frac{\exp(\beta_0) \cdot \exp(\beta_1)}{\exp(\beta_0)} = \exp(\beta_1)$$

Post term delivery and age

We know that the age distribution among the two groups of women is different - the women giving birth for the first time will on average be younger!

It might be relevant to compare the two groups after "adjustment for age".

We will start by modeling the association between post term delivery and age among the **women with Parity==0**.

The simplest **logistic regression model** is:

$$\log(\text{odds}) = \alpha_0 + \alpha_1 \cdot \text{Age} \quad \text{odds} = \exp(\alpha_0) \cdot \exp(\alpha_1)^{\text{Age}}$$

To get a sensible reference age:

$$\log(\text{odds}) = \alpha_0 + \alpha_1 \cdot (\text{Age} - 30) \quad \text{odds} = \exp(\alpha_0) \cdot \exp(\alpha_1)^{\text{Age}-30}$$

Post term delivery and age (Parity==0)

$$\log(\text{odds}) = \alpha_0 + \alpha_1 \cdot (\text{Age} - 30) \quad \text{odds} = \exp(\alpha_0) \cdot \exp(\alpha_1)^{\text{Age}-30}$$

$$\text{Age} = 30: \log(\text{odds}) = \alpha_0 \quad \text{odds} = \exp(\alpha_0)$$

$$\text{Age} = 31: \log(\text{odds}) = \alpha_0 + \alpha_1 \quad \text{odds} = \exp(\alpha_0) \cdot \exp(\alpha_1)$$

$$\text{Age} = 18: \log(\text{odds}) = \alpha_0 - 12 \cdot \alpha_1 \quad \text{odds} = \exp(\alpha_0) \cdot \exp(\alpha_1)^{-12}$$

$$\text{Age} = 19: \log(\text{odds}) = \alpha_0 - 11 \cdot \alpha_1 \quad \text{odds} = \exp(\alpha_0) \cdot \exp(\alpha_1)^{-11}$$

$$\text{Age} = 25: \log(\text{odds}) = \alpha_0 - 5 \cdot \alpha_1 \quad \text{odds} = \exp(\alpha_0) \cdot \exp(\alpha_1)^{-5}$$

$$OR_{31 \text{ vs } 30} = \exp(\alpha_0) \cdot \exp(\alpha_1) / \exp(\alpha_0) = \exp(\alpha_1)$$

$$OR_{19 \text{ vs } 18} = \exp(\alpha_0) \cdot \exp(\alpha_1)^{-11} / (\exp(\alpha_0) \cdot \exp(\alpha_1)^{-12}) = \exp(\alpha_1)$$

$$OR_{25 \text{ vs } 19} = \exp(\alpha_0) \cdot \exp(\alpha_1)^{-5} / (\exp(\alpha_0) \cdot \exp(\alpha_1)^{-11}) = \exp(\alpha_1)^6$$

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Post term delivery and age (Parity==0)

$$\log(\text{odds}) = \alpha_0 + \alpha_1 \cdot (\text{Age} - 30) \quad \text{odds} = \exp(\alpha_0) \cdot \exp(\alpha_1)^{\text{Age}-30}$$

We saw: $\text{Age} = 30: \text{odds} = \exp(\alpha_0)$

$$OR_{31 \text{ vs } 30} = \exp(\alpha_1)$$

$$OR_{19 \text{ vs } 18} = \exp(\alpha_1)$$

$$OR_{25 \text{ vs } 19} = \exp(\alpha_1)^6$$

That is,

$\exp(\alpha_0)$ is the odds in the reference ($\text{Age} == 30$)

$\exp(\alpha_1)$ is the OR for 1 year difference.

and

$$OR_{\text{6 years}} = OR_{\text{1 year}}^6$$

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Post term delivery and age (Parity==0)

Using a computer we get:

| | CI | | | H = 0 | | |
|--------|---------|--------|---------|---------|--------|---------|
| | est | se | lower | upper | z | p |
| Const | -0.8446 | 0.0332 | -0.9096 | -0.7795 | -25.44 | <0.0001 |
| Age-30 | 0.0207 | 0.0071 | 0.0069 | 0.0345 | 2.93 | 0.003 |

| | CI | | | H = 1 | | |
|--------|--------|----|--------|--------|--------|---------|
| | est | se | lower | upper | z | p |
| Const | 0.4297 | | 0.4027 | 0.4586 | -25.44 | <0.0001 |
| Age-30 | 1.0209 | | 1.0069 | 1.0351 | 2.93 | 0.003 |

Note, only the estimates and the confidence intervals should be transformed!

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Post term delivery and age (Parity==0)

| | CI | | | H = 1 | |
|--------------------|--------|--------|--------|--------|---------|
| | est | lower | upper | z | p |
| Odds if Age=30 | 0.4297 | 0.4027 | 0.4586 | -25.44 | <0.0001 |
| One years age dif. | 1.0209 | 1.0069 | 1.0351 | 2.93 | 0.003 |

From odds to probability:

$$\Pr(\text{post term if } \text{Age} == 30) = \frac{0.4297}{1 + 0.4297} \left(\frac{0.4027}{1 + 0.4027}; \frac{0.4586}{1 + 0.4586} \right) \\ = 30.1(28.7; 31.4)\%$$

Five years age difference:

$$OR_{\text{5 years}} = 1.0209^5 (1.0069; 1.0351)^5 \\ = 1.11(1.03; 1.19)$$

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Post term delivery and age (Parity==0) - Formulations

Methods

The risk of post term delivery among women giving birth for the first time was described by a logistic regression model with age as a continuous variable. ...

Results

We found that five year age difference corresponds to an odds ratio of 1.11(1.03; 1.19). A 30 year old woman giving birth for the first time has 30(29;31)% risk of post term delivery.

Conclusion

The risk of post delivery among women giving birth for the first time increases with the age of the woman....

Logistic regression checking the model

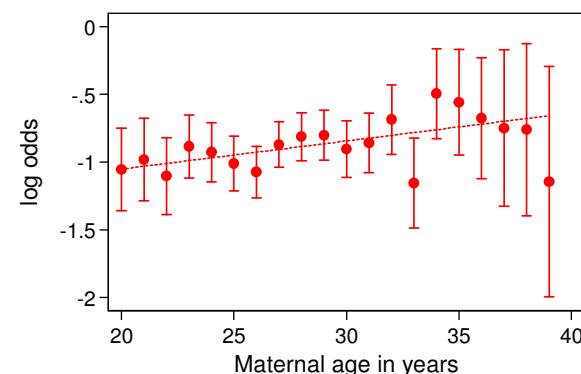
It is outside the scope of this course to go into details on how to check the model, so we will just state the assumptions behind the model:

1. All the observations should be **independent**.
2. There is exactly the same **two possible outcomes** for each observation.
3. The log odds is a **linear function** of age.

The last assumption can to some extend be checked by plotting the fitted regression line and the observed odds (with 95% CI) for each distinct age.

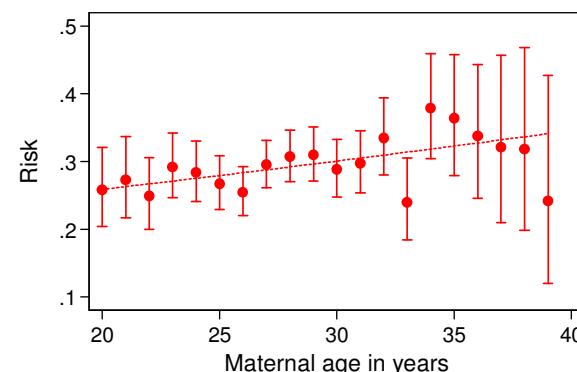
Post term delivery and age (Parity==0)

$$\log(\text{odds}) = \alpha_0 + \alpha_1 \cdot (\text{Age} - 30)$$



Post term delivery and age (Parity==0)

$$\text{risk} = \frac{\exp(\alpha_0 + \alpha_1 \cdot (\text{Age} - 30))}{1 + \exp(\alpha_0 + \alpha_1 \cdot (\text{Age} - 30))}$$

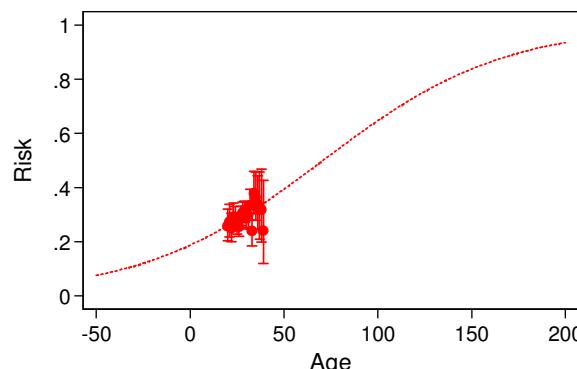


Not linear! But almost

Post term delivery and age (Parity==0)

Extrapolating we see the non-linearity.

$$\text{risk} = \frac{\exp(\alpha_0 + \alpha_1 \cdot (\text{Age} - 30))}{1 + \exp(\alpha_0 + \alpha_1 \cdot (\text{Age} - 30))}$$



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Post term delivery parity adjusting for age

We now know that

- The risk of post term delivery **increases with age** (among women with **parity==0**).
- The risk of post term delivery is **smaller for Parity>0**.
- Women with **Parity>0** are older.

From this we can deduce that **adjusting for age** (if reasonable) will **increase** the difference between the two parity groups.

We now show how to find an age adjusted estimate, when we assume a linear "effect" of age on log odds.

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Post term delivery and age

We fit the same model to the **Parity>0** group and then look at the difference:

| log odds | Slope | | | | log odds Age==30 | | | |
|------------|-------|-------|--------|-------|------------------|-------|--------|--------|
| | est | se | lower | upper | est | se | lower | upper |
| Parity>0 | 0.025 | 0.007 | 0.012 | 0.039 | -1.037 | 0.029 | -1.093 | -0.981 |
| Parity==0 | 0.021 | 0.007 | 0.007 | 0.035 | -0.845 | 0.033 | -0.910 | -0.780 |
| Difference | 0.005 | 0.010 | -0.015 | 0.024 | -0.193 | 0.044 | -0.279 | -0.107 |

The **standard errors** of the differences are found as usual:

$$\text{se}(est_{\text{parity}>0} - est_{\text{parity}==0}) = \sqrt{\text{se}_{\text{parity}>0}^2 + \text{se}_{\text{parity}==0}^2}$$

We see that we can assume the slopes to be identical, we could also test the hypothesis:

$$z = \frac{0.005 - 0}{0.010} = 0.5 \quad p = 64\%$$

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Post term delivery and age – assuming identical slopes

If we assume identical the slopes, then we can write the model:

$$\log(\text{odds}) = \gamma_0 + \gamma_1 \cdot (\text{Age} - 30) + \gamma_2 \cdot \text{Par1}$$

$$\text{odds} = \exp(\gamma_0) \cdot \exp(\gamma_1)^{(\text{Age}-30)} \cdot \exp(\gamma_2)^{\text{Par1}}$$

We see that

$\exp(\gamma_0)$ is the odds among 30-year old with **Parity==0**.

$\exp(\gamma_0) \cdot \exp(\gamma_1)$ is the odds among 30-year old with **Parity>0**.

$\exp(\gamma_1)^A$ is the odds ratio for the age difference **A** years among women in the same **Parity** group.

$\exp(\gamma_2)$ is the odds ratio comparing **Parity>0** to **Parity==0**, at the same age.

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Post term delivery and age - assuming identical slopes

The model is easily fitted by a computer:

| log odds | Slope | | | | log odds Age==30 | | | |
|------------|-------|-------|-------|-------|------------------|-------|--------|--------|
| | est | se | lower | upper | est | se | lower | upper |
| Parity>0 | 0.023 | 0.005 | 0.013 | 0.033 | -0.036 | 0.029 | -1.092 | -0.981 |
| Parity==0 | | | | | -0.839 | 0.031 | -0.900 | -0.778 |
| Difference | 0 | | | | -0.197 | 0.043 | -0.281 | -0.114 |

The age adjusted OR comparing Parity>0 to Parity==0:

$$OR_{10} : \exp(-0.197) (\exp(-0.281); \exp(-0.114)) = 0.821 (0.755; 0.892)$$

and if we compare Parity==0 to Parity>0:

$$OR_{01} : \frac{1}{0.821} \left(\frac{1}{0.892}; \frac{1}{0.755} \right) = 1.22 (1.12; 1.32)$$

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Post term delivery and Parity - Formulations

Methods

The risk of post term delivery among women was modeled by a logistic regression model with age as a continuous variable....

Results version1

Comparing Parity >0 to Parity==0 the crude odds ratio was 0.87(0.81;0.95). The age adjusted odds ratio was 0.82(0.76;0.89).

Results version2

Comparing Parity==0 to Parity>0 the crude odds ratio was 1.14(1.06;1.24). The age adjusted odds ratio was 1.22(1.12;1.32).

Conclusion ??

Women giving birth for the first time have up to 32% higher odds (risk) of post term delivery compared to other women of the same age.

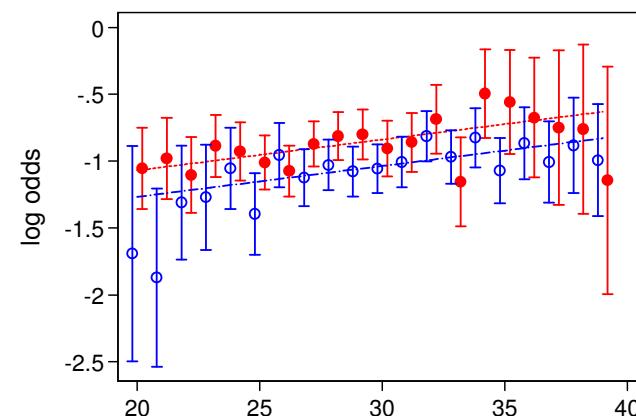
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Post term delivery and age - assuming identical slopes

$$\log(\text{odds}) = \gamma_0 + \gamma_1 \cdot (\text{Age} - 30) + \gamma_2 \cdot \text{Par1}$$



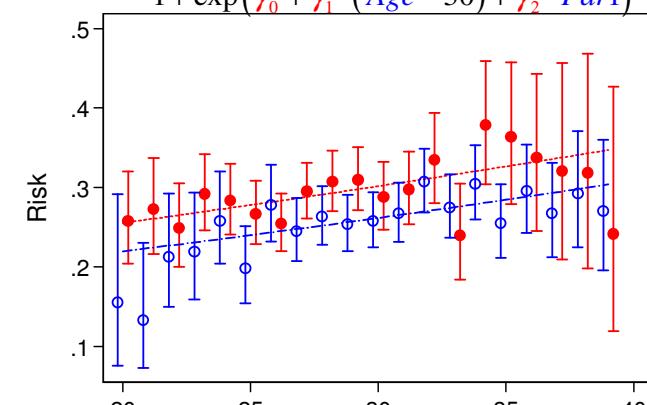
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Post term delivery and age - assuming identical slopes

$$\text{risk} = \frac{\exp(\gamma_0 + \gamma_1 \cdot (\text{Age} - 30) + \gamma_2 \cdot \text{Par1})}{1 + \exp(\gamma_0 + \gamma_1 \cdot (\text{Age} - 30) + \gamma_2 \cdot \text{Par1})}$$



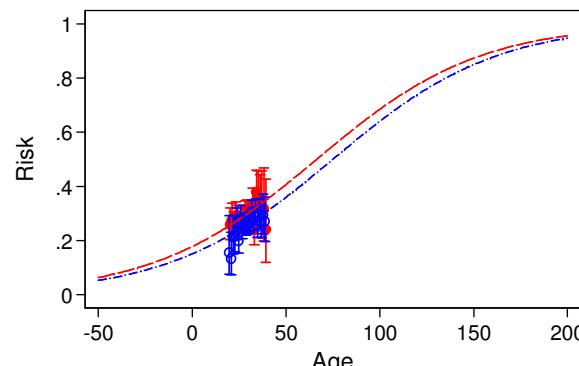
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Post term delivery and age - assuming identical slopes

$$\text{risk} = \frac{\exp(\gamma_0 + \gamma_1 \cdot (\text{Age} - 30) + \gamma_2 \cdot \text{Parl})}{1 + \exp(\gamma_0 + \gamma_1 \cdot (\text{Age} - 30) + \gamma_2 \cdot \text{Parl})}.$$



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Why use logistic regression

There is a **long tradition** for using logistic regression when considering binary outcome. Some of the reasons are:

It is the **mathematical nicest** model for binary outcome, and hence the **first** type of models that was included in the statistical software.

If you have a **case-control** design, then you want to work with odds ratios.

If the **event is rare**, then it will give you **relative risk** estimates.

It is one of the few models for binary data that ensures that the estimated probability is **between zero and one**.

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Linear and logistic regression - a comparison

In a **linear regression** the **outcome is continuous**:
Lung function, Blood pressure, BMI, concentrations...

In a **logistic regression** the **outcome is binary**:
Post term delivery, gender, dead/alive, sick/ well, BMI>30..
Neither of the models make **any assumptions** about the **explanatory variable**!!
In both models they can be continuous, binary or categorical.

In **both models** we have to assume **independence** between observations.

In **both models** we assume linearity -
of expected value or the log odds.

Both models are readily fitted by standard statistical packages.

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Regression models in general - why? Adjustment

You have now looked at two of the most commonly used regression models in their most simple forms, involving one continuous and one binary explanatory variable.

You have seen how one can use such models for **adjustment**: What is the 'effect' of the binary 'exposure' when **adjusting** for the continuous variable?

Exactly the same models could answer the question:
What is the 'effect' (slope) of the **continuous** 'exposure' when **adjusting** for the binary variable?
E.g. what is the increase in risk of post term delivery associated with age when we **adjust** for parity?

Often one has several explanatory variables, a mixture of continuous, binary and categorical and the purpose is to **adjust for more than one**.

In such case one might apply a **multiple regression model**.

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Regression models in general - why? Effect modification

We have also seen how we could compare the 'effect' of one explanatory variable for subgroups described by another explanatory variable (**effect modification**):

What is the difference in the PEFR-height relationship for men and women?

What is the difference in the Risk-age relationship for the two parity groups?

Typically by **comparing the slopes**.

Often one has several explanatory variables, a mixture of continuous, binary and categorical and the purpose is to **model effect modification** between explanatory variables.

In such case one might apply a **multiple regression** model.

Regression models in general - why? Prediction

We could also have used exactly the same models for **prediction/prognosis**:

What is the expected PEFR for a person with a given sex and a given height?

What is the risk of post term delivery for women of a given age having her first child?

Often one has several explanatory variables, a mixture of continuous, binary and categorical and the purpose is to make **prediction** for a person with a given set of characteristics.

In such a case one might apply a **multiple regression** model.